



Galaria, Empresa Pública
 de Servizos Sanitarios

Hospital do Meixoeiro

DOSE-CALCULATION ALGORITHMS USED IN RADIATION TREATMENT PLANNING

MANUEL SALGADO FERNÁNDEZ

Servicio de Radíofísica y Protección Radiológica Galaria. Hospital do Meixoeiro. Av. Meixoeiro s/n, 36200 Vigo (PONTEVEDRA). Tlf: 986 811712. Fax: 986 8111 99



SANTIAGO DE COMPOSTELA 20-05-10



1895 X-ray discovery
Two months (!!!) after the discovery of xrays the 1st patient was treated with radiation therapy.
Rose Lee a 65 year old woman with breast cancer

 Treating physician was a Chicago *medical student* named Emil Grubbe



1896 Antoine Henri Becquerel: discovery of radioactivity
Interaction with a film
Interaction with the human body



Discovery of polonium and radium
Pierre Curie: uranium salt on his skin
Burned skin
Donation of radioactive material to hospitals

Medical Record

A Weekly Journal of Medicine and Surgery

Vol. 64, No. 16. Whole No. 1719.

NEW YORK, OCTOBER 17, 1903.

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Original Articles.

RADIUM: WITH A PRELIMINARY NOTE ON RADIUM RAYS IN THE TREATMENT OF CANCER.*

By MARJARET A. CLEAVES, M.D., NEW YORK,

for only the scientific world, but the lay as well, stens with bated breath to the marvelous ales of radium; tales which, especially when acompanied by demonstrations of the apparently tagical phenomena of this new element, seem more effitting fairy lore than abstruse scientific fact; and ne can but wonder whether radium may not prove veritable Aladdin's lamp to medical science as well s to physics

"All nature is vibrating, from the lowest musical ote to the highest pitch of the chemical rays," and tradium the highest form of etheric vibration is to In 1898 Prof. Pierre Curie and Mme. Sklodowska Curie, when investigating the radiations from uranium discovered by Becquerel, found that some samples of pitchblende or uraninite, from which uranium is extracted, gave forth radiations much more powerful than any uranium they had found, having four times the activity of metallic uranium.

Painstaking research of a substance associated w it very much in its chemic substance Mme. Curie ga in honor of Poland, the la

Polonium is to be had in the form of a subnitrate resembles particles of nic white powder. The on polonium in this country J. Hammer, from whose monograph¹ on radium r





No units
1912 M.Curie: mgh
1910 Ci
1914 mg destroyed
1933 Failla and Quimby: TED (Threshold erithema dose). SED

Types of Dose-Calculation Algorithms

Data-driven algorithmsModel-driven algorithms



INPUT:
-EXPERIMENTAL DATA OF A GREAT NUMBER OF SITUATIONS.
-MATHEMATICAL FITS.
-INTERPOLATION-EXTRAPOLATION.

ADVANTAGES:

 THE METHOD PROVIDES THE MOST ACCURATE REPRODUCTION OF THE BEAM FOR IDENTICAL CONDITIONS TO THOSE OF MEASUREMENT.

-BEAM COMMISSIONING IS EASY.

DISADVANTAGES:
 -VERY SIMPLE AND LIMITED GEOMETRIES.
 -ONLY WATER AS MEDIUM.

INPUT:

 -EXPERIMENTAL DATA OF FUNDAMENTAL PROCESSES.

 -MATHEMATICAL MODELS OF THE RADIATION FIELD.

 ADVANTAGES:
 -MORE FLEXIBILITY IN REPRODUCING BEAMS CONFIGURATIONS FOR WHICH MEASUREMENTS HAVE NOT BEEN TAKEN.
 -CAPABILITY OF MODELING THE PATIENT.

DISADVANTAGES:
-APPROXIMATION TO REALITY. INADEQUACIES OF THE MODEL.
-COMMISSIONING PROCEDURE MAY BE COMPLEX

Capability of modeling the beam
Capability of modeling the patient
Ease of beam commissioning
Accuracy of dose calculation
Speed of dose calculation

The dose calculation algorithm must accurately model all beam configurations normally used in the clinic

- Treatment machine, beam energy
- Beam geometry

 Treatment portal definition: symmetric, asymmetric collimation, MLC, customized blocks, electron applicators, skin collimation

Beam modifiers: physical wedge, dynamic wedge, compensators, bolus

No system models all configurations

Ingenuity required to develop suitable workarounds: i.e. different SSD's models.

The dose calculation algorithm must accurately model the patient
 External surface anatomy
 Heterogeneous internal anatomy
 Based on high-resolution, pixel-based CT data

The dose calculation must be fast
Goal: real-time calculation and display
Reality: more sophisticated dose model
Work-arounds
Background calculation
Fast calculation option

PURE MATRICIAL

SIMPLEST FORM= TO LOOK-UP TABLE POLAR COORDINATES

-ADECUATE FOR ISOCENTRIC TECHNIQUES

 -SO MANY REPRESENTATIONS AS ISOCENTER DEPTHS AND FIELD SIZES ARE NEEDED

 -QUICK LOST OF RESOLUTION BEYOND ISOCENTER

Tsien, K.C. 1955 "The application of automatic computing machines to radiation treatment planning". Brit.J.Radiol. 28: 432.





- -CARTESIAN SYSTEM
- ADECUATE FOR FIXED-SSD TECHNIQUES
- -SO MANY REPRESENTATIONS AS FIELD SIZES ARE NEEDED
- -SIMPLEST AND INTUITIVE
- -UNIFORM RESOLUTION
 - -PENUMBRA ZONES POORLY REPRESENTED

Sterling T D , Perry H, Katz I. 1964 "Automation of radiation treatment planning".Brit.J.Radiol.37: 544.



DECREMENTAL LINE SYSTEM

- LINES WITH DISTANCE TO AXIS GIVEN BY THE POINT OF THE PROFILE WITH AN ESTABLISHED DECREASING DEPTH-DEPENDING PATTERN.
- -SO MANY REPRESENTATIONS AS FIELD SIZES ARE NEEDED
- -ADECUATE FOR REFLECTING DOSE VARIATIONS IN AND OUTSIDE THE BEAM AXIS.
- -PENUMBRA ZONES WELL REPRESENTED.

Orchard, P.G. 1964 "Decrement lines: a new presentation of data in cobalt-60 beam dosimetry". Brit.J.Radiol.37: 756



FAN LINE SYSTEM

- INTERSECTIONS AMONG HORIZONTAL LINES AND RAYS DIVERGING FROM THE SOURCE.
- -SO MANY REPRESENTATIONS AS FIELD SIZES ARE NEEDED.
- -IRREGULAR STEPS=ADJUSTABLE RESOLUTION
- -GOOD REPRESENTATION OF PRIMARY RADIATION.
- -USED IN POSTERIOR ANALYTICAL METHODS.
- Cunningham , J.R. and Milan , J. 1969 "Radiation treatment planning using a display-oriented small computer". Computer in Biomedical Research, Vol III,,Stacy R.W. and Waxman B.C. Eds.(Academic Press).New York.
- Bentley, R.E. and Milan, J. 1971 "An interactive digital computer system for radiotherapy planning".Brit.J.Radiol.44: 826 .

SEMIEMPIRICAL: ANALYTICAL REPRESENTATIONS OF THE BEAM

$D(x,y,z) = P(z,z_{ref}) \bullet g_Z(x,y)$

 $P(z,z_{ref})$

Dose at depth *z* relative to *z_{ref}*(PDD)

 $g_{z}(x,y) = g_{1,z}(x) \cdot g_{2,z}(y)$

Relative value in point (x, y) at depth z

SEMIEMPIRICAL: ANALYTICAL REPRESENTATIONS OF THE BEAM

$$P(z, x_{eq}) = 10 \left[az + b + (cz + d) \log x_{eq} \right] \quad x_{eq}^2 = \frac{UV}{2(U+V)}$$

Relation area-perimeter in a field of U x V size (equivalent square formula)

Relation between position xand field size X

PARAMETERS TO ADJUST: a, b, c, d, o

Sterling T D , Perry H, Katz I. 1964 "Automation of radiation treatment planning". Brit.J.Radiol.37: 544.

Polinomial series:

$$P(z,F;A) = \sum_{0}^{3} a_{i} z^{i}$$

(ai tabulated for different squared fields and SSDs)

Van de Geijn, J. 1965 "The computation of two and three dimensional dose distributions in cobalt 60 teletherapy", Brit. J. Radiol. 38: 369.

 $\mu(\mathbf{c}) = \mu_{o} - \mathbf{a} [1 - \exp(-\mathbf{b} \cdot \mathbf{c})]$

PARAMETERS TO ADJUST: *a*, *b*, μ0

$$P(z,F;A) = 100 \cdot \left(\frac{F + z_m}{F + z}\right)^2 \cdot \exp\left[-\mu(c) \cdot (z - z_m)\right]$$

- F: SSD
- zm: reference depth
- c: side of the squared field of area A

Van de Geijn J, Chien IC, Pocheng C, Frederickson HA. 1980 "A unified 3-D model for external beam dose distributions" Umegaki Y, ed. Computers in radiation therapy. Proceedings of the Seventh International Conference of the Use of Computers in Radiotherapy, Tokyo; 203-207.



 $OAR(d, x, FS_1)$

- Milan J, Bentley RE. 1974 "The storage and manipulation of radiation dose data in a small digital computer".Br J Radiol. Feb;47(554):115-21.
- DATA FOR SQUARED FIELDS ADJUSTED TO A PRODUCT OF CENTRAL-AXIS DEPTH DOSE AND OFF-AXIS PROFILE IN A FAN-LINE GRID:
- -17 points for PDD and 47 for every profile at dmax, 5, 9, 13 and 17 cm depth
 - -Data for PDD stored as infinite distance ("without" inverse squared distance dependence or SSD):
 - SSD1: source-surface distance of the base fielddmax: depth at the peak absorbed dose
 - FS1: field sized: depth

Profiles as function of the off-axis position x

DOSE CALCULUS IN NON-REFERENCE SITUATIONS:

$$D(d, x, FS_2) = PDD_{\infty}(d, FS_2) * OAR(d, x', FS_1) * \left[\frac{(SSD_1 + d_{\max})}{(SSD_2 + d)}\right]^2$$

 $FS_2 = FS_1 * (SSD_2 / SSD_1)$

Field size FS_1 projected to SSD_2

 $X^* = X * (SSD_2 / SSD_1)$

Distance x projected to SSD_2

CORRECTIONS:



2) Heterogeneities correction:

• Equivalent Path Length

 $d' = \frac{1}{\rho_w} \int_0^z \rho(x) \, dx$

 ρ_w : water electronic density $\rho(x)$: electronic density at point x

With d' a correction factor (CF) can be defined:

 $CF(d) = e^{-\mu_w(d'-d)}$

Method of the effective linear attenuation



Method of the Tissue-Air-Ratio (TAR) ICRU Report 24. 1976 "Determination of Absorbed Dose in a Patient Irradiated by Beams of X or Gamma Rays in RT Procedures".

$$CF(d) = \frac{PDD(fs, d', SSD)}{PDD(fs, d, SSD)} \left(\frac{SSD + d'}{SSD + d}\right)^2$$

$$CF(d) = \frac{PDD(fs, d - n(d - d'), SSD)}{PDD(fs, d, SSD)}$$

phantoms".Br J Radiol. May;38:378-85

Method of the effective SSD

Cunningham JR, Shrivastava PN, Wilkinson JM. 1972 "Program IRREG-calculation of dose from irregularly shaped radiation beams" Comput Programs Biomed. Apr;2(3):192-9.

Method of the isodose line displacement Greene D, Stewart JG. <u>1965</u> "Isodose curves in non-uniform

Heterogeneities correction:





$\mathsf{TAR}(d, r_d) = D_d / D_{fs}$

 $\mathsf{TMR}(d, r_d) = D_d / D_{t_{max}}$

-Multiplicative properties of the TAR: a material with twice the electronic density of another attenuates twice than the later. -Effect of different effective Z is taken into account with absorption coefficients μ_{en} ratios.

Batho's Method

El-Khatib E, Battista JJ. 1984 "Improved lung dose calculation using tissue-maximum ratios in the Batho correction" .*Med Phys;11(3):279-86*

$$CF = \frac{(\mu_{en} / \rho)_N}{(\mu_{en} / \rho)_w} * \prod_{m=1}^N (TMR(d - d_m + d_{max}))^{(\mu_m - \mu_{m-1}) / \mu_w}$$

Generalized Batho's formula

where μ_m are the attenuation coefficients of the m-th slice and d_m the distance from the anterior surface of the heterogeneity to the point. -Definition of TAR, which is replace by TMR in the most advanced version of the formula.

Based on the O'Connor's Theorem:

"The ratio of secondary and primary photon fluences is constant for two different mediums if every distance including field sizes are scaled inversely to the density." O'Connor J E 1957 "The variation of scattered x-rays with density in an irradiated body" Phys. Med. Biol. 1 352–69

This means that an analogous TAR quantity can be obtained for phantoms with non-equivalent to water materials scaling the depth and field size.

• Equivalent TAR (ETAR) Method

Sontag MR, Cunningham JR. 1978 "The equivalent tissue-air ratio method for making absorbed dose calculations in a heterogeneous medium". Radiology. Dec;129(3):787-94.

$$CF = \frac{TAR_{hetero}(d', fs')}{TAR_{agua}(d, fs)}$$

where d' are the Equivalent Path Length and fs' a effective field size, which can be compute through a effective radius $r'=r^*\rho'$, where r is the radius of the equivalent circular field and ρ' a effective electronic density:



Every weight W_{ijk} is function of the distance and the angle from the voxel *ijk* to the point of interest. It also depends on the photon fluence.

3) Wedges: Same procedure as in open fields but with the corresponding profiles (OARs). As an alternative:

 $W(x,y) = \exp(-\mu \cdot c(x,y))$

μ linear attenuation coefficient c(x,y) thickness crossed by radiation

4) Irregular fields and off-axis point:

Clarkson JR. 1941 "A note on depth dose in fields of irregular shape". Br. J. Radiol 14, 265

$$Dp = D_{air}(d, r) * \left[TAR(d', 0) * P_p + SAR(d)_p \right]$$

where:

 D_p : Dose at point p $D_{air}(d,r)$: Dose in air at point p (depth=*d* and off-axis distance= *r*) *d'*: effective depth (fan line depth)

$$P_{p} = t + \sum_{j} \left(G_{j} * (1-t) \right)^{*} \Delta \theta_{j} / 2\pi * \sum_{i} \left(1 - (1 + \alpha r_{i} / p) * e^{\left(\frac{-\alpha r_{i}}{(p)}\right)} \right)$$

$$SAR(d)_{P} = \sum_{i} SAR(d, \mathbf{r}_{i})^{*} \sum_{j} G_{j} \Delta \theta_{j} / 2\pi$$

Clarkson's method:



-Irregular fields as sums of sectors of circular fields

-Separation of scatter and primary components. Definition of scatter-air ratio for a field size *r* and depth *z* :

SAR(z,r) = TAR(z,r) - TAR(z,0)

-Transmission coefficient of collimator given by t

Clarkson's method:

-Perimeter of the irregular field composed by vectors such as the sign of the contribution of the sector is given by:

$$G = (\vec{v}_1 \times \vec{v}) / |\vec{v}_1 \times \vec{v}|$$



-Distribution of radiation at a point r' of the source:

$$\frac{\alpha^2}{2\pi(p)^2} * e^{\left(\frac{-\alpha r'}{(p)}\right)}$$

Disadvantages Bentley-Milan-Clarkson:

-Poorer results for simplex conditions than pure matrix models

-Does not account for scatter near block boundary.

-Block transmission not necessary true transmission.

-Does not explicitly support dynamic wedge.

-Variations in scatter radiation due to oblique incidence not considered.

-Poor modeling of multileaf collimators (MLC) where configurations are very different from circular fields.

MODEL-DRIVEN ALGORITHMS: BOLTZMANN TRANSPORT EQUATION

 $\vec{\Omega} \cdot \nabla \varphi + \mu \cdot \varphi = \int_{dT'} \int_{4\pi} \mu' \cdot \varphi' \cdot d\Omega' \cdot dT' + \mathbf{Q}(\vec{\mathbf{r}}, \mathbf{T}, \vec{\Omega})$

 $\varphi(\mathbf{T}, \vec{\Omega}, \vec{r}, t)$ Particle fluence

- Q(v,r,t) Sources contribution
- $\mu = \mu(\mathbf{r}, \mathbf{T})$ Interaction coefficient

Rigorous model of the physical interactions that can be solved exactly.

 $\mathbf{T} \mathbf{y} \mathbf{\Omega}$ Energy and direction of the particles

Too much complex for using in clinic for the moment. However recently, there are promising and remarkable works:

-M. Frank, M. Herty, M. Schäfer: Optimal Treatment Planning in Radiotherapy Based On Boltzmann Transport Calculations. Math. Mod. Meth. Appl. Sci. 18 (2008) 573-592. -M. Frank, M. Herty, A.N. Sandjo: Optimal Radiotherapy Treatment Planning Governed by Kinetic Equations to appear in Math. Mod. Meth. Appl. Sci. (2009)

MODEL-DRIVEN ALGORITHMS: CONVOLUTION

ONVOLUTION $D(\vec{r}) = \int \frac{\mu}{\rho} (E) \cdot \Psi(\vec{r}') \cdot K(\vec{r} - \vec{r}') dv dE$

where:

 μ/ρ : linear attenuation coefficient $\Psi(r)$: Photon fluence at point r K(r): Kernel of energy deposition at point r (Dose in water at point *r* per unit total released energy by photon at point 0)



MODEL-DRIVEN ALGORITHMS: CONVOLUTION

 $D(\vec{r}) = \int \frac{\mu}{\rho} (E) \cdot \Psi(\vec{r}) \cdot K(\vec{r} - \vec{r}) dv dE$

Using Terma we take into account different released energies at point *r* due to differences in composition at that point. Better results than using only fluence at point *r*.



MODEL-DRIVEN ALGORITHMS: CONVOLUTION

 $D(\vec{r}) = \int \frac{\mu}{\rho} (E) \cdot \Psi(\vec{r}) \cdot K(\vec{r} - \vec{r}) dv dE$

Convolution algorithm is fast and uses the Fast Fourier Transform:

Operations for N³ points: N⁶

N³ log₂ N

Inverse Fourier Transform Fourier Transform of the Terma of the beam

The same input for every beam

 $D(r) = \mathfrak{I}^{-1}(\mathfrak{I}(T(r)) * \mathfrak{I}(\mathbf{K}(r)))$

Inverse Fo

MODEL-DRIVEN ALGORITHMS: SUPERPOSITION

$$\mathsf{D}(\vec{r}) = \int \frac{\mu}{\rho} (\mathsf{E}) \cdot \Psi(\rho \cdot \vec{r}') \cdot \mathsf{K}(\rho \cdot (\vec{r} - \vec{r}')) dv d\mathsf{E}$$

Based on: Convolution algorithm calculates the dose at point r-r' using a deposition kernel in water at point 0 whatever the composition of the medium is between points r-r' and origin. In the Superposition Algorithm rescaling the

integration variable by the electronic density heterogeneities are taken into account in a better way. However the energy deposition kernel is still data "in water".

No FFT can be used but other speeding up procedures have been developed like the collapsed cone convolution. It also allows taking into account "kernel tilting" with beam divergence.



ENERGY DEPOSITION KERNELS

Mackie T R, Bielajew A F, Rogers D W O and Battista J J 1988 "Generation of photon energy deposition kernels using the EGS Monte Carlo code" Phys. Med. Biol. 33 1–20

Point spread function

Pencil Beam



13.64–73

Ahnesjo A 1984 "Application of transform algorithms for calculation of absorbed dose in photon beams Int. Conf. On the Use of Computers in Radiation Therapy", VIII ICCR (Toronto, Canada) (Los Alamos, CA: IEEE ComputerSociety Press) pp 17–20

Planar spread function

Mohan R, Chui C and Lidofsky L 1986 "Differential pencil

beam dose computation model for photons" Med. Phys.

MONTE CARLO ALGORITHMS

A particle is viewed as a random sequence of free flights that end with an interaction event where the particle changes its direction of movement, loses energy and, occasionally, produces secondary particles.

Numerical generation of random histories

 $\lambda_{\rm T} \equiv \left(\mathcal{N} \sigma_{\rm T} \right)^{-1}$

Mean free path between interactions



Probability of occurring an event type A after an interaction

ULTIMATE ALGORITHM BASED ON FUNDAMENTAL PROCESSES DATA

PENELOPE, GEANT4, EGS4, MCNP



STATE OF THE ART

accurate calculation of the Dose
calculations using radiobiological models
heterogeneus prescription inside the target
4D- virtual simulation
Gating or tracking
High conformation: SRS, IMRT

STATE OF THE ART

but we do not know still how the treatment was delivered......
Organ movements
Setup errors
Intrafraction movements
Daily situation of the linac
Errors

.

and will require the greatest dosimetric accuracy. At this point, a 5% change in dose may result in a 10% to 20% change in tumor control probability at a TCP of 50%. Similarly, a 5% change in dose may result in a 20% to 30% impact on complication rates in normal tissues. The results mentioned above refer to changes caused by homogeneous dose distributions covering the whole tumor or organ at risk considered, which is characterized by certain D_{30} and γ values. Nevertheless, they demonstrate the potential impact that a certain change in dose to the clinical outcome may have.

TISSUE INHOMOGENEITY CORRECTIONS FOR MEGAVOLTAGE PHOTON BEAMS

Report of Task Group No. 65 of the Radiation Therapy Committee of the American Association of Physicists in Medicine

pist (i.e., radiation oncologist) suspected the error. No striking reaction was observed on the other (non-gynecological) patients.

Thus it could be concluded that at least a 7% difference in dose delivered is manifested in the patient's response to radiation treatment and is detectable clinically by a radiation oncologist.

Members

 Nikos Papanikolaou (Chair) University of Arkansas, Little Rock, Arkansas
 Jerry J. Battista London Regional Cancer Centre, London, Ontario, Canada Arthur L. Boyer Stanford University, Stanford, California
 Constantin Kappas University of Thessaly, Medical School, Larissa, Hellas
 Eric Klein Mallinckrodt Institute of Radiology, St. Louis, Missouri
 T. Rock Mackle University of Wisconsin, Madison, Wisconsin
 Michael Sharpe Princess Margaret Hospital, Toronto, Ontario, Canada
 Jake Van Dyk London Regional Cancer Centre, London, Ontario, Canada

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NEXT FUTURE

attempts with new devices to calculate the delivered dose:





NEXT FUTURE



NEXT FUTURE

We need to know delivered dose
Probably using the portal image.





V; cos(a; ± w+) + € cos((+= $\overline{P}^{x} = \overline{\xi} \overline{\psi}_{i}^{x} + 2 \overline{\xi} \overline{\xi} \overline{\psi}_{i}^{x}$ $\int \chi(t) dt = \frac{\chi(t)}{dt} = ((\omega)^{2})^{2}$ $(1 - \frac{1}{\sqrt{2}})^{2} \frac{\partial^{2} u}{\partial t^{2}} + \frac{\partial^{2} u}{\partial x^{2}} + \frac{\partial^{2} u$ $= \int \left(\frac{9\lambda}{2\pi} + \frac{2\pi\gamma}{\Xi\lambda}\right) \tan k$ $= \int \left(\frac{4}{2\pi} + \frac{2\pi\gamma}{\Xi\lambda}\right) \tan k$ $= \int \left(\frac{4\pi\gamma}{\Xi\lambda}\right) \tan k$